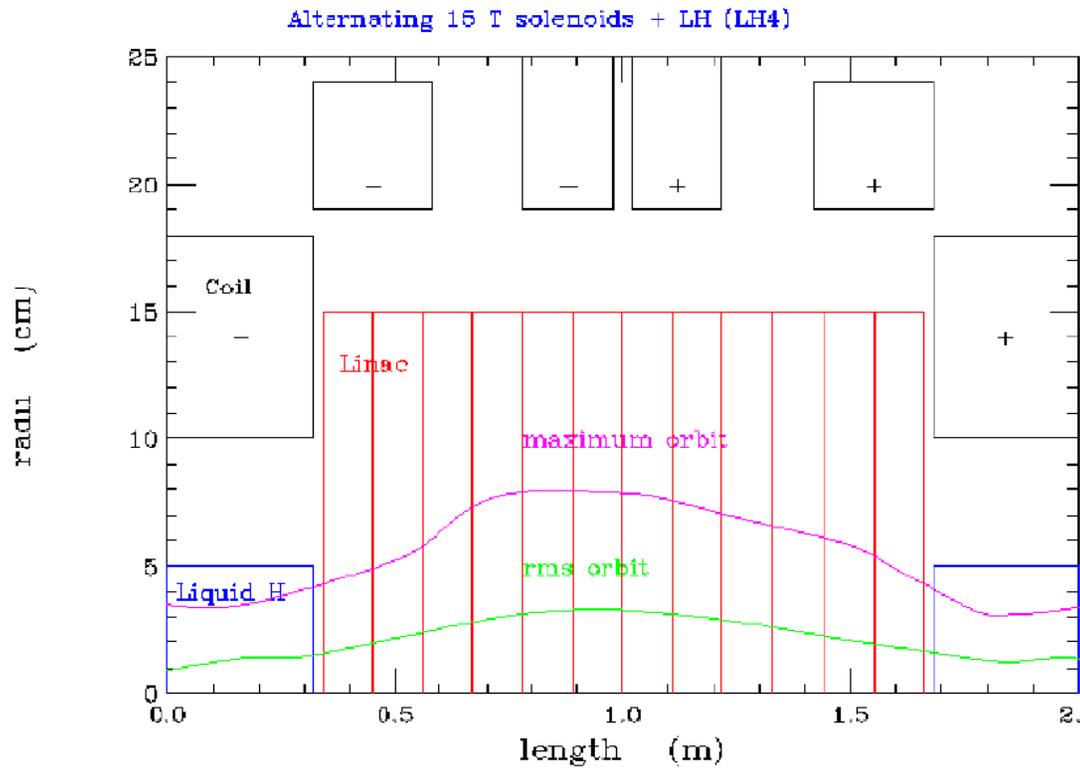


Longitudinal Cross Section of a Muon Cooling Module

Transverse ionization:
$$\frac{d\varepsilon_N}{ds} = -\frac{\varepsilon_N}{\beta^2 E} \frac{dE}{ds} + \frac{\beta \gamma \beta_f}{2} \frac{d\langle \theta_{rms}^2 \rangle}{ds}$$

cooling

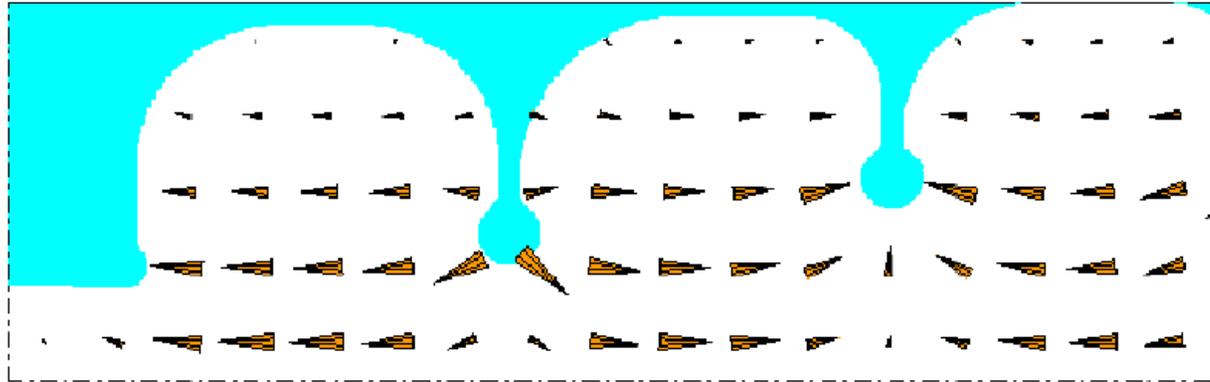


RF Specifications of the Cavity System

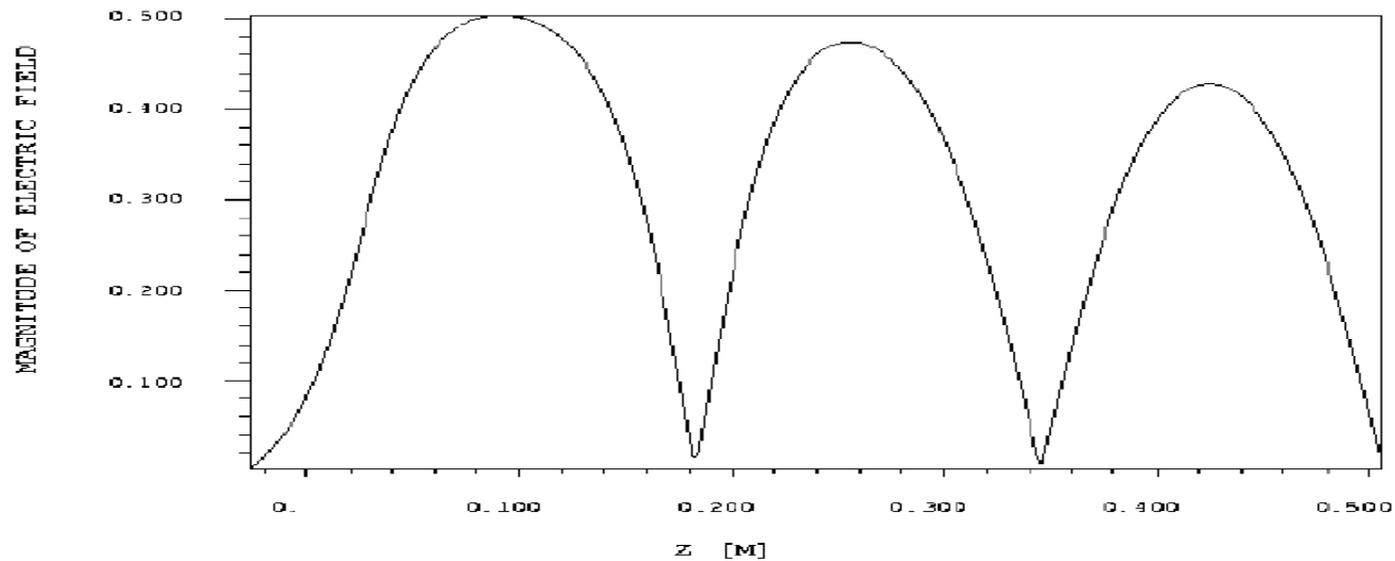
- **Cavity**
 - frequency (MHz) = 805
 - shunt impedance Z_t^2 (M Ω /m) = 17.2
 - quality factor Q_0 = 32800
 - filling time (μ s) = 6.5
 - transit time factor = 0.76
 - power (MW/m) for 30 MV/m = 30
- **High power coupler**
 - critical coupling $\beta = 1$
- **Transition waveguide**
 - reflected power < 1 % of incident power
 - bandwidth > 1 % of 805 MHz

MUCOOL Cavity: Open Iris Standing Wave Structure (one half of the structure is shown)

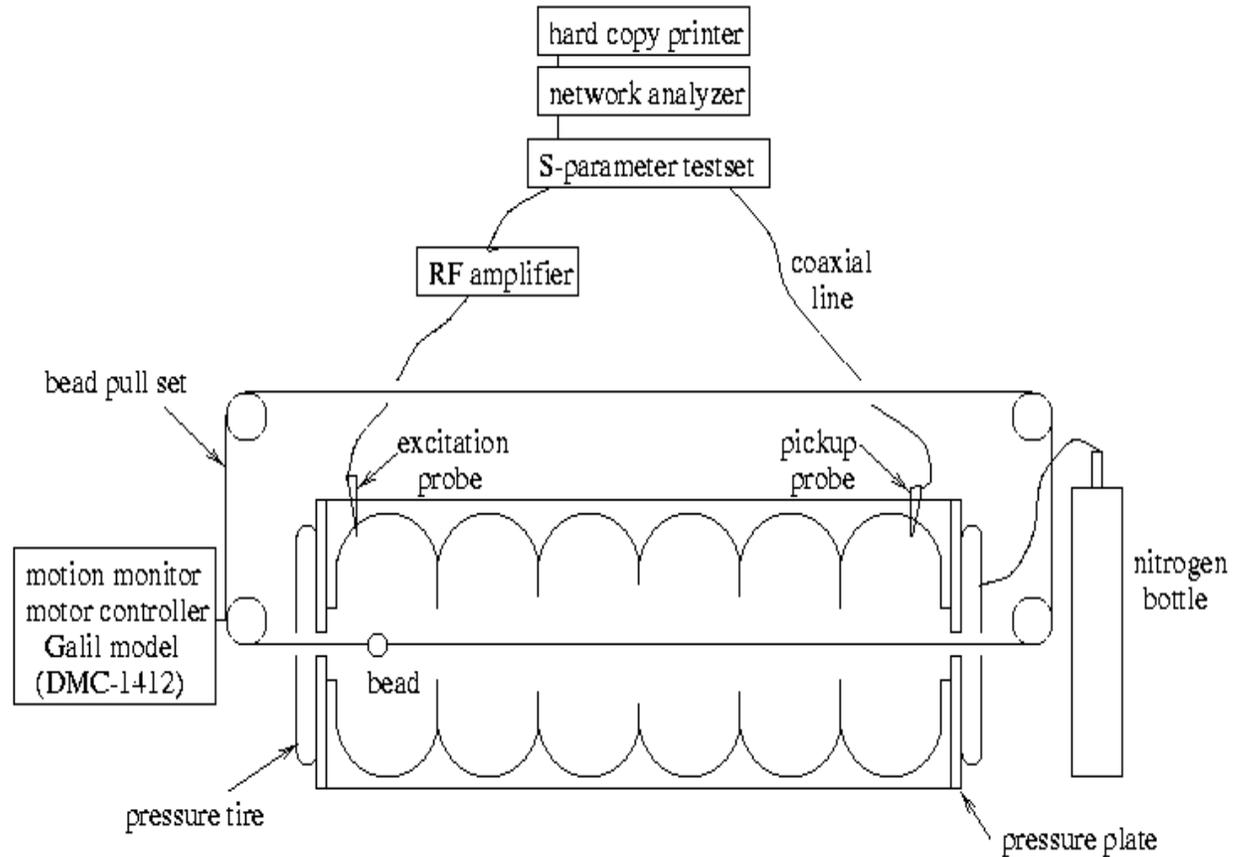
Acceleration π Mode



On Axis Electric Field



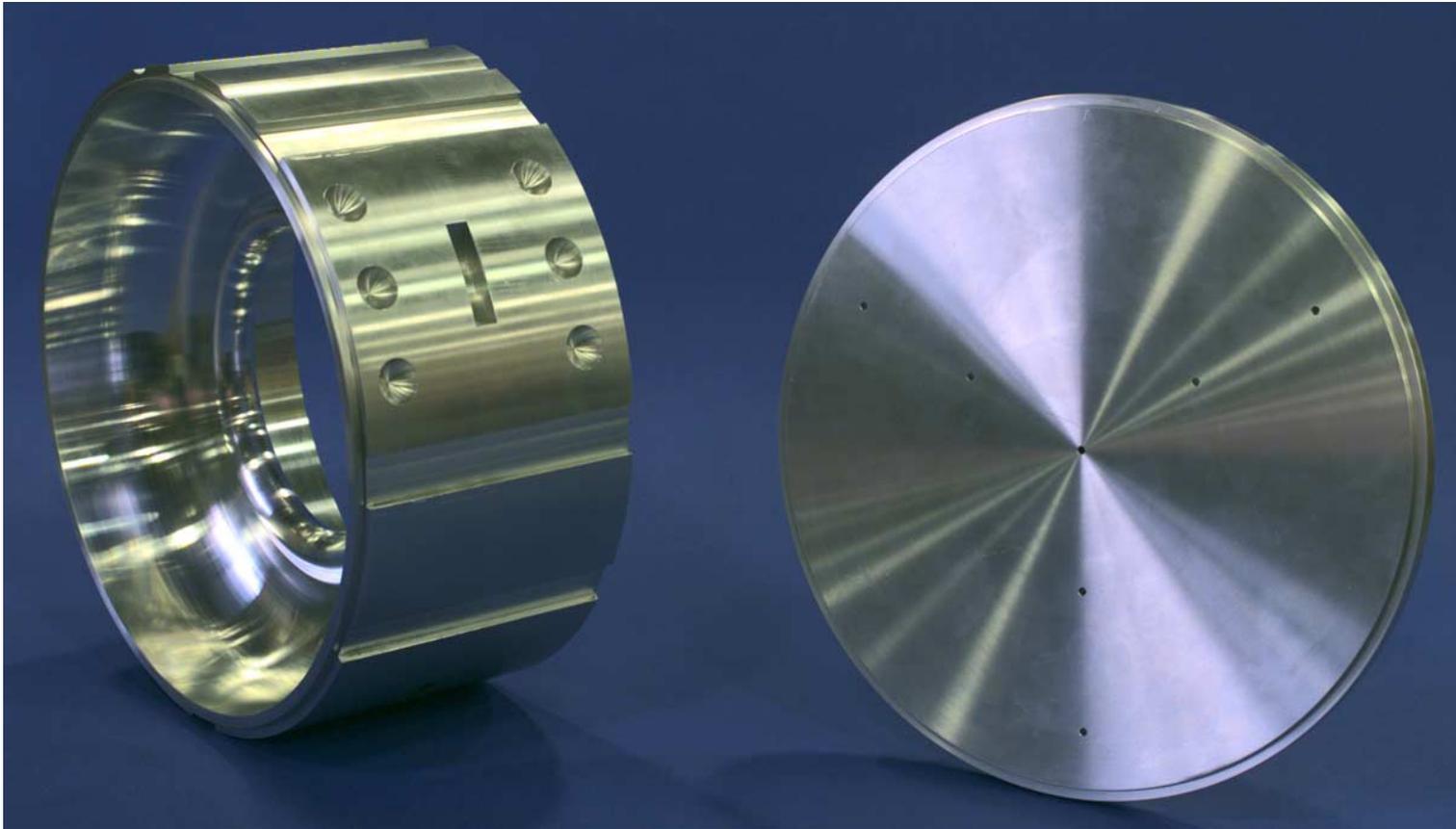
Schematics of Low Power Test Setup



RF Cavity System (Aluminum Model)

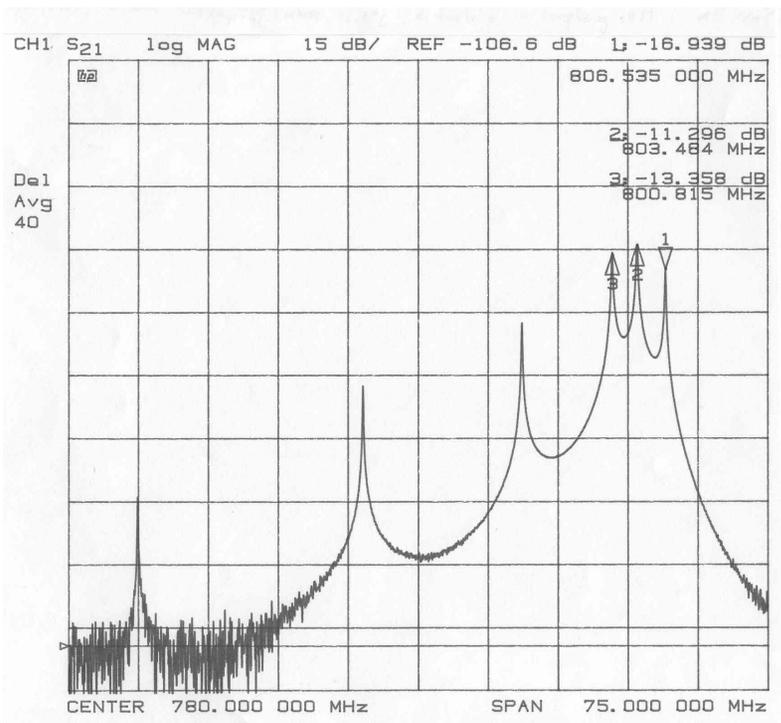


Two-Half Cell Aluminum Cavity

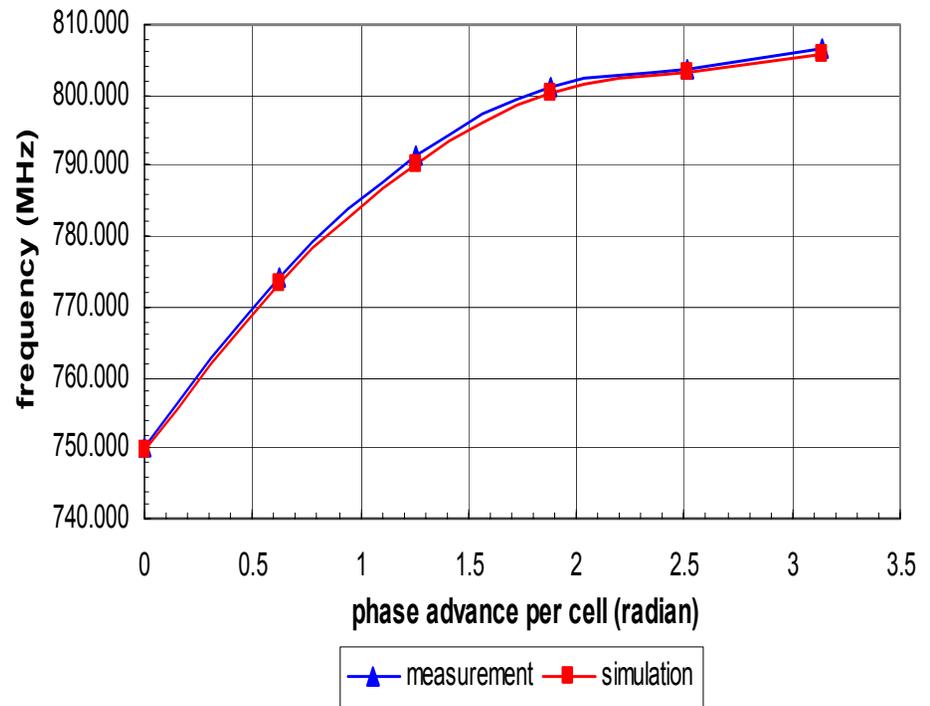


First Passband of TM Modes (Acceleration Modes) Spectrum

Transmission Amplitude vs. Frequency



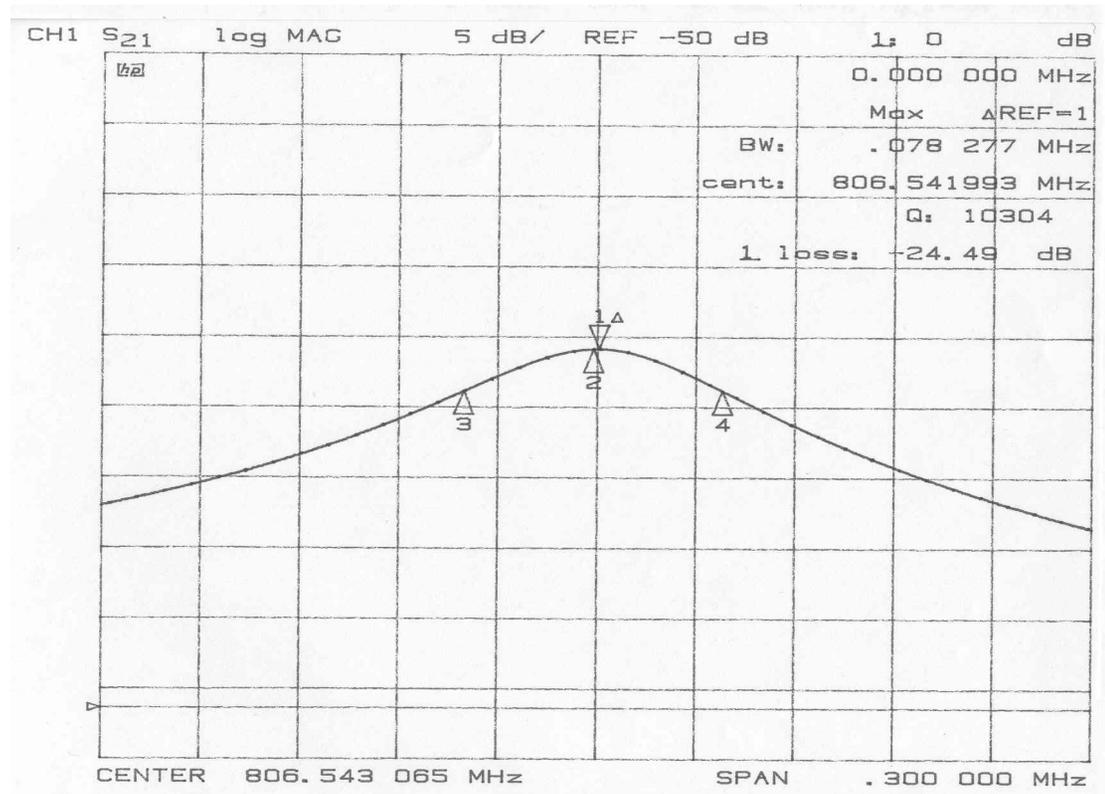
Dispersion Relation



Disagreement: $\sim 0.1\%$ or 0.8 MHz

Q Measurement of the Acceleration π Mode

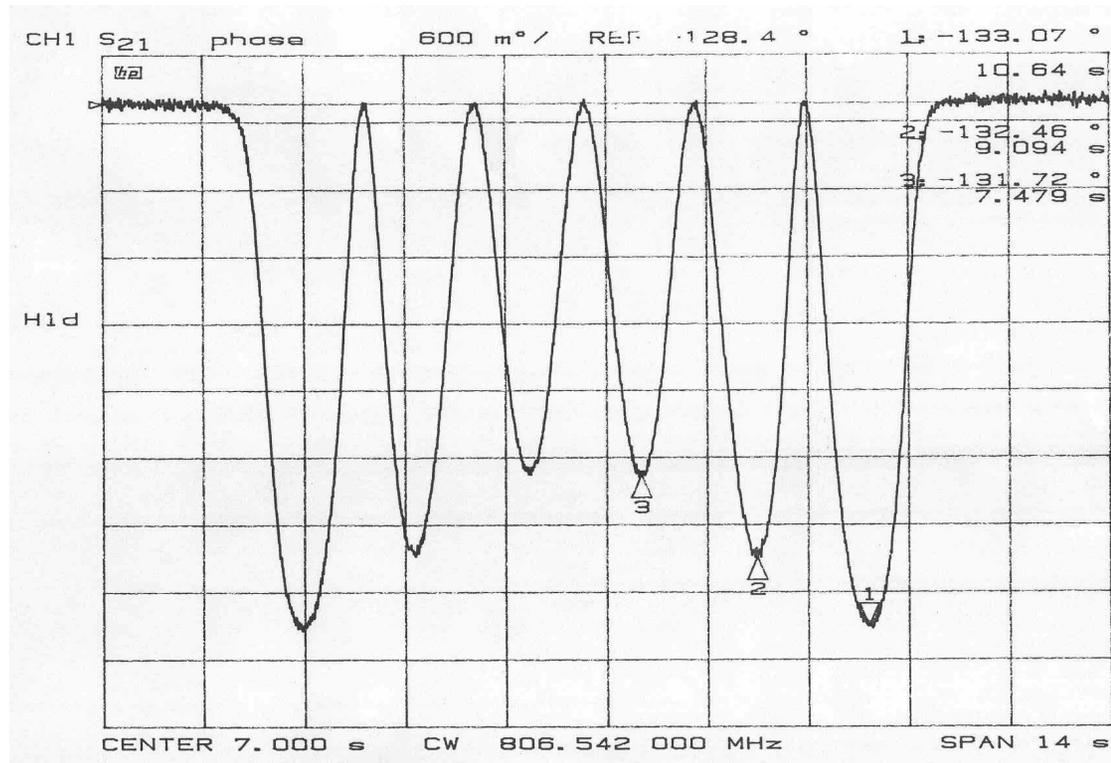
Transmission Amplitude vs. Frequency



Bead Pull Measurement of the Electric Field of the π Mode

Bead pull:
$$\frac{\delta\omega}{\omega_0} = -\frac{3v}{4U_T} \left(\frac{\epsilon_r - 1}{\epsilon_r + 2} \epsilon_0 E^2 + \frac{\mu_r - 1}{\mu_r + 2} \mu_0 H^2 \right) \quad \frac{\delta\omega}{\omega_0} \propto \delta\phi \propto E^2$$

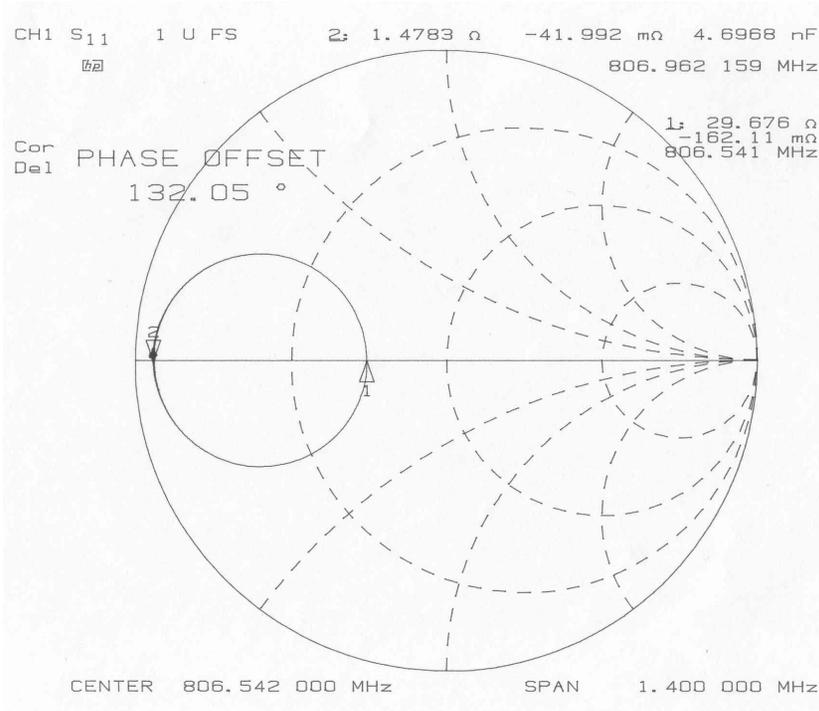
Transmission Phase vs. Time



Coupling Coefficient β Measurements

Smith chart: an example of external coupling measurement

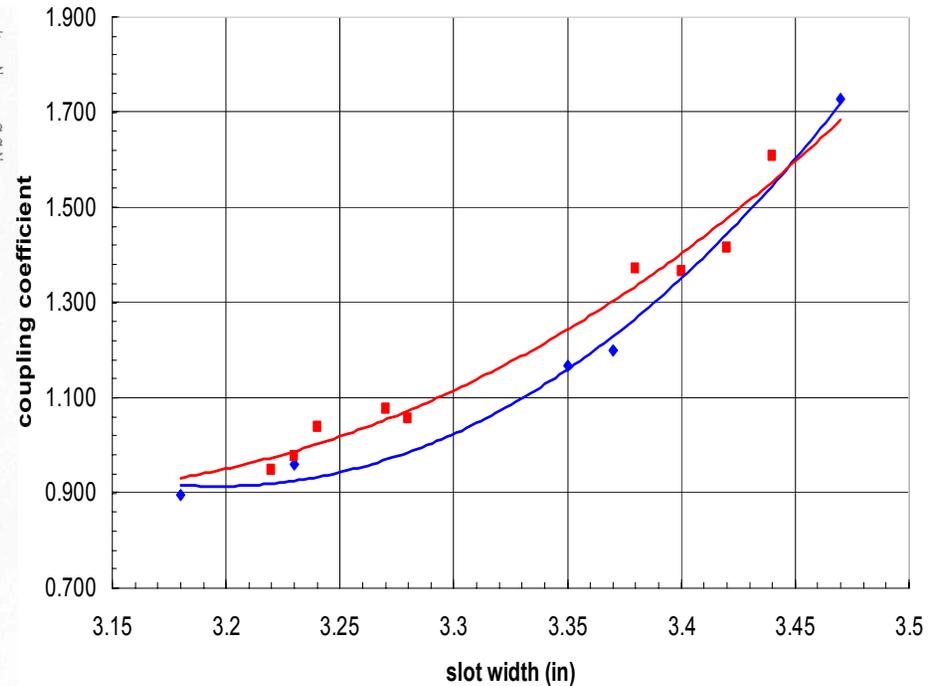
Reflection Coefficient



Measurement: $\beta = \frac{r}{50\Omega} = 0.594$

Simulation: $\beta = 0.584$

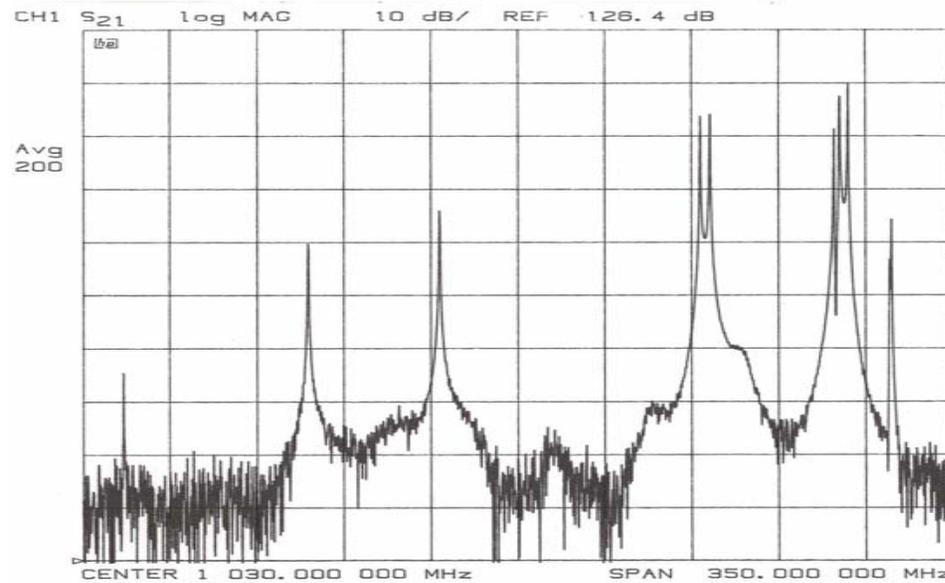
Simulation:
$$\beta = \frac{P_{ext}}{P_w} = \frac{(1/2) \int (\vec{E}x\vec{H})_l ds}{(R_s/2) \int \vec{H}^2 ds}$$



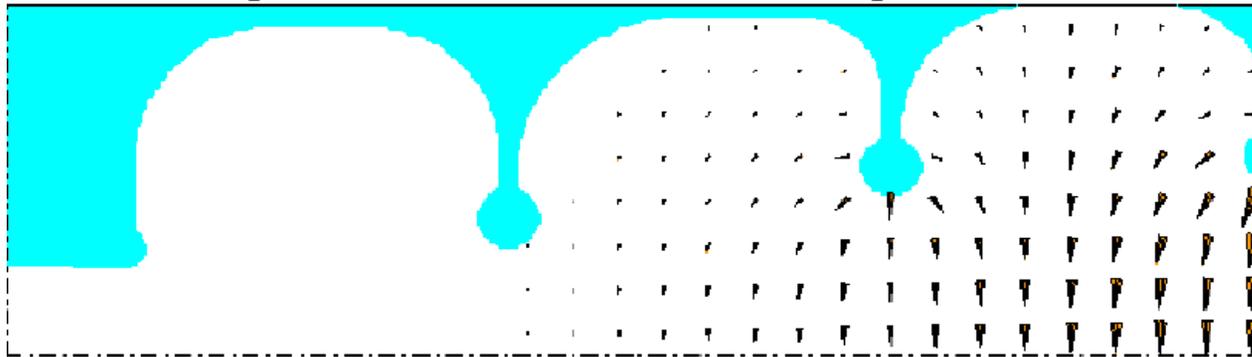
◆ simulation ■ measurement — Poly. (simulation) — Poly. (measurement)

Disagreement: <10 %

Higher Order Cavity Modes: First Ten Dipole Modes



Example: Electric Field of the First Dipole Mode



Simulated frequency = 874.676 MHz

Measured frequency = 871.608 MHz

Comparison Between Simulations and Measurements

	measurement	simulation	disagreement
frequency (MHz)	806.542	805.687	0.1%
Q	10304	10650	3%
coupling coefficient	0.594	0.584	2%

On Axis Electric Field

cell	1	2	3	4	5	coupling
measurement	1.186	1.106	1.000	1.000	1.103	1.191
simulation	1.176	1.108	1.000	1.000	1.108	1.176
disagreement	2 % or less					

Copper Cavity After Brazing



Copper Cavity Measurements Before Tuning

frequency (MHz)	804.996
Q	16774
coupling coefficient	1.053

cell	1	2	3	4	5	coupling
field strength	1.156	1.093	1.000	1.000	1.086	1.102

- Field level in coupling cell is off by ~ 6%.
- Fine tuning corrects the discrepancy to 1% level.

Future Plans for High Power Test at Lab G

- First, condition cavity with superconducting solenoid turned off.
- Study high voltage breakdown in the cavity.
 - Measure incident and reflected klystron powers as a function of time.
 - Measure charges from the cavity.
 - Monitor vacuum behavior.
- Measure field gradients.
- Study the behaviors of the cavity and the superconducting solenoid when both are on.

Lab G: superconducting solenoid



805 MHz klystron



Low Power Test
Of The
MUCOOL
High Gradient
RF Cavity Vincent Wu